

C.U.SHAH UNIVERSITY

Summer Examination-2016

Subject Name: Partial Differential Equations

Subject Code: 5SC02MTC2

Branch: M.Sc.(Mathematics)

Semester: 2

Date: 06/05/2016

Time: 10:30 To 1:30

Marks: 70

Instructions:

- (1) Use of Programmable calculator and any other electronic instrument is prohibited.
- (2) Instructions written on main answer book are strictly to be obeyed.
- (3) Draw neat diagrams and figures (if necessary) at right places.
- (4) Assume suitable data if needed.

SECTION – I

- Q-1 Attempt the Following questions (07)**
- a. Solve: $(D^2 - D')z = 0$. (02)
 - b. Find the particular integral of $(D^2 + 2DD' + D'^2)z = \sin(2x + 3y)$. (02)
 - c. Classify the partial differential equation $r + 4s + 4t = 0$. (02)
 - d. Find the solution of $\frac{\partial^2 z}{\partial x^2} = 0$. (01)
- Q-2 Attempt all questions (14)**
- a. Reduce the equation $r + 2s + t = 0$ to canonical form. (06)
 - b. Solve: $(D^3 - 6D^2D' + 11DD'^2 - 6D'^3)z = e^{5x+6y}$. (05)
 - c. Eliminate the arbitrary functions f and g from $z = f(x^2 - y) + g(x^2 + y)$. (03)
- OR**
- Q-2 Attempt all questions (14)**
- a. Reduce the equation $4r = t$ to canonical form and hence solve it. (06)
 - b. Solve: $r - t = x - y$. (05)
 - c. Eliminate the arbitrary functions f and F from $y = f(x - at) + F(x + at)$. (03)
- Q-3 Attempt all questions (14)**
- a. Find the particular integral of $(D^2 - D'^2 + D - D')z = e^y(x - 1)$. (05)
 - b. Solve: $x^2r + 2xys + y^2t = 0$. (05)
 - c. Solve: $(D^3 + 3D^2D' - 4D'^3)z = 0$. (04)
- OR**
- Q-3 Attempt all questions (14)**
- a. Solve the equation $\frac{\partial u}{\partial x} = 2\frac{\partial u}{\partial t} + u$ by the method of separation of variables. (05)
 - b. Solve: $r + s - 6t = y \cos x$. (05)
 - c. Prove that $F(D, D')e^{ax+by} = F(a, b)e^{ax+by}$, where a and b are constants. (04)



SECTION – II

- Q-4 Attempt the Following questions (07)**
- What is equipotential surface? (02)
 - Write Dirichlet problem for a Circle. (02)
 - Write the general form of equation for which the method of changing variable $u = \log x, v = \log y$ can apply. (02)
 - $u = x^2 - y^2$ is solution of two dimension Laplace equation. State whether the statement is true or false? (01)
- Q-5 Attempt all questions (14)**
- In usual notation, prove that $\frac{\partial^2 u}{\partial r^2} + \frac{1}{r} \frac{\partial u}{\partial r} + \frac{1}{r^2} \frac{\partial^2 u}{\partial \theta^2} = 0$. (07)
 - Using Monge's method, solve the equation $x(r + 2xs + x^2t) = p + 2x^3$. (07)
- OR**
- Q-5 Attempt all questions (14)**
- Classify and Reduce the equation $r^2 + y^2t = y$ to canonical form. (07)
 - State and prove Harnack's theorem. (07)
- Q-6 Attempt all questions (14)**
- Using Monge's method, solve the equation $r - t = 0$. (07)
 - Show that the solution of three dimensional wave equation $\nabla^2 u = \left(\frac{1}{c^2}\right) \left(\frac{\partial^2 u}{\partial t^2}\right)$ can be put in the form $e^{\pm i(lx + my + nz + kct)}$, provided $k^2 = l^2 + m^2 + n^2$. (07)
- OR**
- Q-6 Attempt all Questions (07)**
- Using Monge's method, solve the equation $3r + 4s + t + (rt - s^2) = 1$. (07)
 - Find general solution of heat equation $\frac{\partial^2 u}{\partial x^2} = \frac{1}{k} \frac{\partial u}{\partial t}$ by the method of separation of variables. (07)

